STUDY MODULE DESCRIPTION FORM								
Name of the module/subject Stochastic methods and mathematical statistics					Code 1010342621010347255			
Field of	study			of study Il academic, practical		r /Semester		
Matl	nematics			eral academic		1/2		
Elective	e path/specialty		Subject	offered in: Polish	Cou	rse (compulsory, elective)		
Cvcle o	f study:	•	Form of stud	ly (full-time,part-time)		obligatory		
	Second-c	full-time						
No. of h	iours				No.	of credits		
Lectu	re: 30 Classe	s: - Laboratory: 30	Project	/seminars:	-	4		
Status	of the course in the study	program (Basic, major, other)		y-wide, from another	'			
		other		univ	ersity-v			
Educati	on areas and fields of sci	ence and art			and	S distribution (number %)		
the s	ciences		4 100%					
Mathematical sciences						4 100%		
ul. I	Knowledge Skills Social							
	competencies							
The m stocha the stu stocha	ain goal is to acquaint stic processes and to dent will get to know t stic differentials (stocl stic differential equation	a student with the basic concepts gain by the student the ability to c he notion of stochastic integral, wi nastic calculus), and the ability to e on. mes and reference to the	alculate som ill acquire the examine whe	e characteristics of e ability to determi ether some proces	of those p ne the sto s is a solu	rocesses. Furthermore ochastic integrals and ution to a given		
Know	vledge:							
		tion of mathematical theories, can describe phenomena from other of			o construc	ct and analyze simple		
		of the known branches of mather	matics - [K_V	V04]				
Skills			700 mether	notical model of -		unorimont of ron-law		
pheno	mena - [K_U30]	ty space; is able to build and analy						
experi		mples of discrete and continuous cal models in which those distribut						
	3. is able to determine the parameters of distribution function of discrete and continuous random variables; can apply the limit theorems and laws of large numbers to estimate probability of some random variables - [K_U33]							
4. is al sample	ble to use the statisticate - [K_U34]	al characteristics of population and				ate by using a probability		
Socia	al competencies							

Social competencies:

1. is able to accurately formulate questions in order to deepen their understanding of given topic or in order to find the missing pieces of reasoning - [K_K02]

2. understands and appreciates the importance of intellectual honesty in the activities of their own and other people; proceeds ethically - [K_K04]

Assessment methods of study outcomes

Lectures

- Assessment of the knowledge and skills based on the written exam

Classes

- Assessment of the knowledge and skills based on tests, which are carried out in the middle of the semester and during the last classes

Course description

Basic concepts of the theory of stochastic processes: stochastic process, sample path of stochastic process, interpretation of a stochastic process as a random variable, interpretation of a stochastic process as a function of two variables, measurability of stochastic process, filtration, class of adapted processes, class of indistinguishable processes, modification of the stochastic process, Kolmogorov's continuity theorem, continuity types of the stochastic process (continuity with probability one, continuity in probability, mean-square continuity).

Probabilistic description of the stochastic process: examples of processes which are analytical defined, some characteristics of sums and products of stochastic processes, canonical form of the stochastic processes, processes with independent increments, telegraphic signals (synchronous processes, asynchronous processes).

Markov process: definition of Markov process, examples of Markov processes, Markov chain, certain examples of the problems of mass service.

Poisson process: definition of Poisson process, properties of Poisson process.

Some characteristics of differentiable processes and integrable processes (convergence in mean-square sense, mean-square derivative, mean-square integral, ergodicity), and elements of spectral analysis of stationary stochastic processes (spectral density).

Martingales: definitions of discrete-time martingale and continuous-time martingale, examples of martingales, verification whether the process is a martingale, transformation of the known stochastic processes to martingales, Doob's martingale inequality, definition of submartingale and supermartingale, example of submartingale and supermartingale in game theory.

Markov time: definition and properties of Markov time, examples of Markov time, definition and example of the first passage time of stochastic process to the set, definition and properties of stopping time, definition and properties of local martingale.

Brownian motion: definition of Brownian motion, definition of standard Brownian motion, properties of standard Brownian motion, properties of sample path of Brownian motion, brownian motion as a square integrable martingale.

Wiener process: definition of Wiener process, Levy's theorem, examples of Wiener processes, Wiener process as a martingale, examples of stochastic processes determined by transformation of Wiener process, which turn out to be a martingales, example of application of the Wiener process into theory of financial mathematics - geometric Brownian motion (exponential Brownian motion).

Construction of Itô integral: white noise, definition of simple function, comparison of the construction of Itô integral with the construction of Riemanna-Stieltjesa integral, non-anticipating processes, predictable processes, Itô isometry, definition of Itô integral, example of calculation of stochastic integral based on the definition of Itô integral, properties of stochastic Itô integral.

Itô formula: definition of Itô process, definition of stochastic differential, definition of diffusion process, Itô's lemma, application of the Itô formula (calculation of stochastic integrals and stochastic differentials, and verification whether some stochastic process is a solution to a given stochastic differential equation).

Applied methods of education:

- lectures - theory presented in connection with the current knowledge of students,

- laboratories - computational experiments.

Basic bibliography:

1. R. Sz. Lipcer, A. N. Sziriajew, Statystyka procesów stochastycznych: filtracja nieliniowa i zagadnienia pokrewne, PWN, Warszawa 1981.

2. A. Pieniążek, J. Weiss, A. Winiarz, Procesy stochastyczne w problemach i zadaniach, Wydaw. Politechniki Krakowskiej im. Tadeusza Kościuszki, Kraków 2000.

3. A. Plucińska, E. Pluciński, Probabilistyka: rachunek prawdopodobieństwa, statystyka matematyczna, procesy stochastyczne, WNT, Warszawa 2000.

Additional bibliography:

1. B. Oksendal, Stochastic differential equations. An introduction with applications, Springer-Verlag, Berlin Heidelberg New York 2000.

2. Z. Brzezniak, T. Zastawniak, Basic stochastic processes. A course through exercises, Springer-Verlag, London 2002.

3. A. Iwanik, J. K. Misiewicz, Wykłady z procesów stochastycznych z zadaniami. Cz. 1: Procesy Markowa, Oficyna Wydaw. Uniwersytetu Zielonogórskiego, Zielona Góra 2009.

Result of average stu	dent's workload	
Activity	Time (working hours)	
1. Participation in lectures		30
2. Participation in classes	30	
3. Preparation for each classes	20	
4. Preparation for written test	12	
5. Assessment classes	4	
6. The written exam		4
7. Consultations	4	
Student's wo	orkload	
Source of workload	hours	ECTS
Total workload	104	4
Contact hours	72	3
Practical activities	30	1